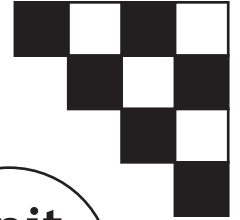


Mathematics 10C



Student Workbook

Unit 4

Graph
 $y = x^2$

x	y
-2	4
-1	1
0	0
1	1
2	4

Lesson 1: Graphing Relations
Approximate Completion Time: 2 Days

Domain
 $\{x \mid -6 < x \leq 3, x \in \mathbb{R}\}$

Range
 $\{y \mid -5 \leq y < 1, y \in \mathbb{R}\}$

Lesson 2: Domain and Range
Approximate Completion Time: 1 Day

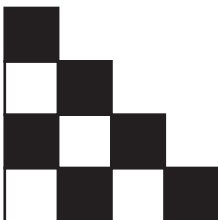
Lesson 3: Functions
Approximate Completion Time: 2 Days

x = 0
y - intercept

y = 0
x - intercept

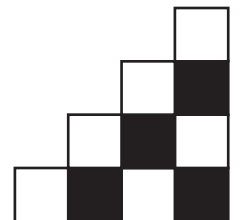
Lesson 4: Intercepts
Approximate Completion Time: 1 Day

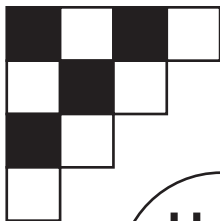
Lesson 5: Interpreting Graphs
Approximate Completion Time: 1 Day



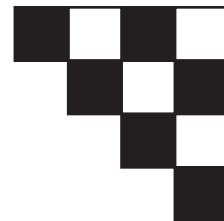
UNIT FOUR

Relations and Functions





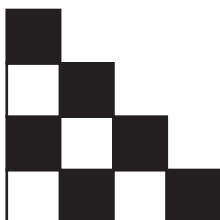
Mathematics 10C



Unit 4

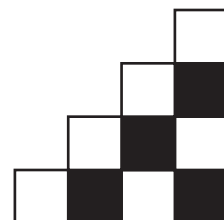
Student Workbook

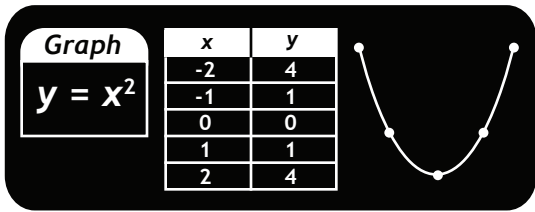
Complete this workbook by watching the videos on www.math10.ca.
Work neatly and use proper mathematical form in your notes.



UNIT FOUR

Relations and Functions





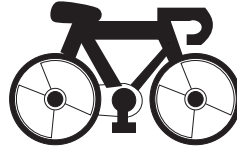
Relations and Functions

LESSON ONE - *Graphing Relations*

Lesson Notes

Introduction Caitlin rides her bike to school every day. The table of values below shows her distance from home as time passes.

a) Write a sentence that describes this relation.



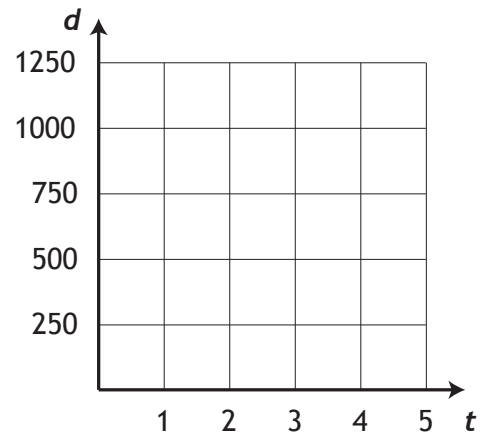
time (minutes)	distance (metres)
0	0
1	250
2	500
3	750
4	1000
5	1250

b) Represent this relation with ordered pairs.

c) Represent this relation with an arrow diagram.

d) Write an equation for this scenario.

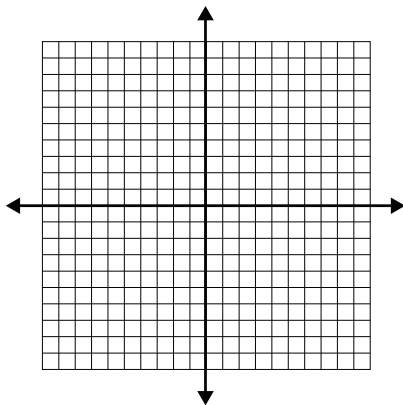
e) Graph the relation.



Example 1 For each relation, complete the table of values and draw the graph.

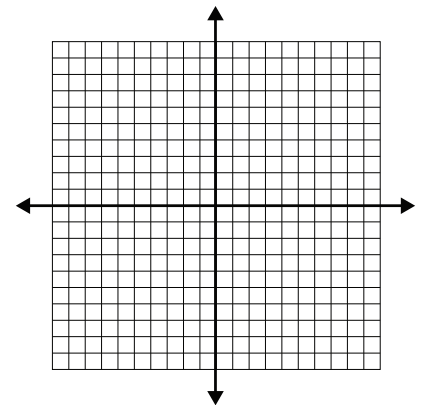
a) $y = -2x + 3$

x	y
-2	
-1	
0	
1	
2	



b) $y = x$

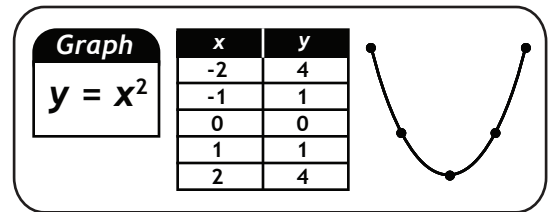
x	y
-2	
-1	
0	
1	
2	



Relations and Functions

LESSON ONE - Graphing Relations

Lesson Notes

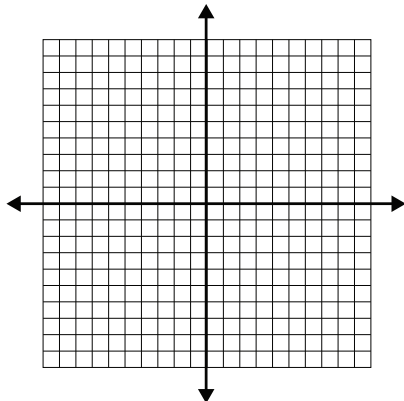


Example 2

For each relation, complete the table of values and draw the graph. State if the relation is linear or non-linear.

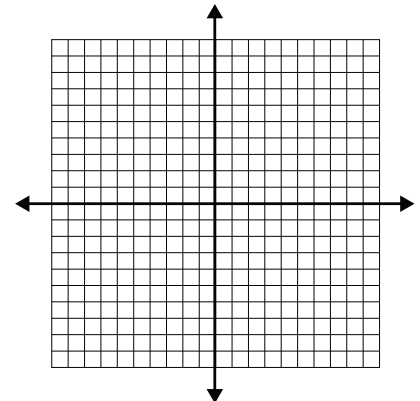
a) $y = x^2$

x	y
-2	
-1	
0	
1	
2	



b) $y = \frac{1}{2}x + 1$

x	y
-4	
-2	
0	
2	
4	



Example 3

For each scenario, state the dependent variable, the independent variable, and the rate. Write the equation.

a) A fruit vendor generates a revenue of R dollars by selling n boxes of plums at \$3 each.

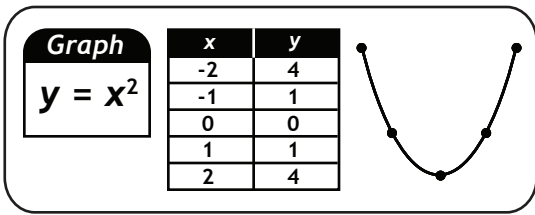
- i) the dependent variable is _____.
- ii) the independent variable is _____.
- iii) the rate is _____.
- iv) the equation is _____.

b) A runner with a speed of 9 m/s can run d metres in t seconds.

- i) the dependent variable is _____.
- ii) the independent variable is _____.
- iii) the rate is _____.
- iv) the equation is _____.

c) A diver experiences a pressure of P kilopascals at a depth of d metres. Underwater pressure increases at 10 kilopascals/metre.

- i) the dependent variable is _____.
- ii) the independent variable is _____.
- iii) the rate is _____.
- iv) the equation is _____.



Relations and Functions

LESSON ONE - Graphing Relations

Lesson Notes

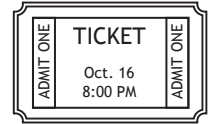
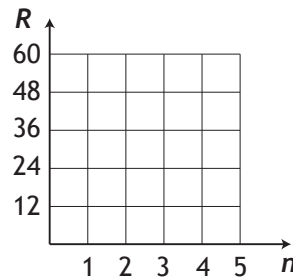
Example 4

Tickets to a concert cost \$12 each. The revenue from ticket sales is R , and the number of tickets sold is n .

- a) Write an equation for this scenario.
- b) Generate a table of values.

n	R

- c) Draw the graph.



- d) Is the relation continuous or discrete?

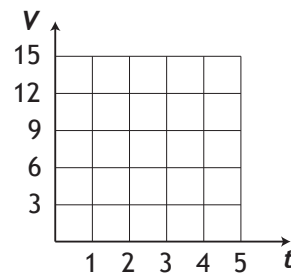
Example 5

A cylindrical tank is being filled with water at a rate of 3 L/min. The volume of water in the tank is V , and the elapsed time is t .

- a) Write an equation for this scenario.
- b) Generate a table of values.

t	V

- c) Draw the graph.



- d) Is the relation continuous or discrete?

Example 6

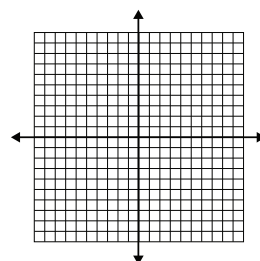
A relation is represented by $4x + 2y = 8$.

- a) Isolate y so this relation can be graphed.

- b) Generate a table of values.

x	y

- c) Draw the graph.

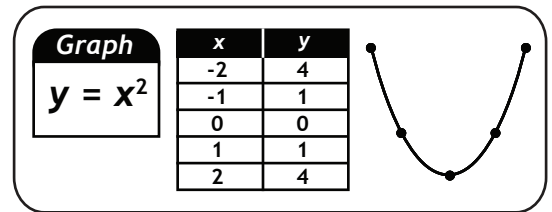


- d) Is the relation continuous or discrete?

Relations and Functions

LESSON ONE - *Graphing Relations*

Lesson Notes



Example 7

Nick, a salesman, earns a base salary of \$600/week plus an 8% commission on sales. The amount of money Nick earns in a week is E , and the total value of his sales is s .

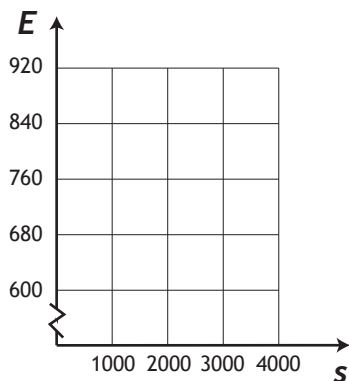


a) Write an equation that relates the variables.

b) Complete the table of values.

s	E
0	
1000	
2000	
3000	
4000	

c) Draw the graph.



d) Is this relation linear or non-linear?

e) Is this relation discrete or continuous?

f) What are the dependent and independent variables?

g) If Nick makes \$6200 in sales one week, what will his earnings be?

h) How much will Nick have to sell if he makes \$1560 in one week?

Domain
 $\{x \mid -6 < x \leq 3, x \in \mathbb{R}\}$

Range
 $\{y \mid -5 \leq y < 1, y \in \mathbb{R}\}$

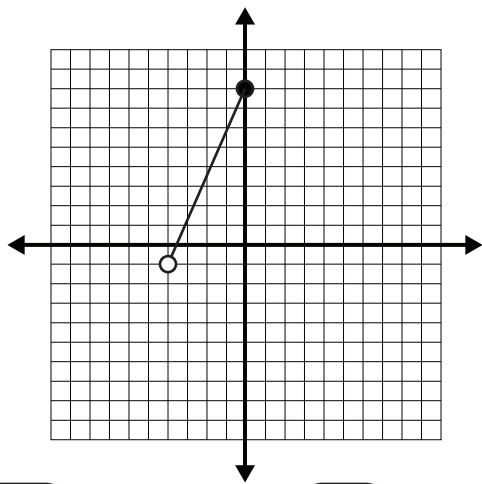
Relations and Functions

LESSON TWO - *Domain and Range*

Lesson Notes

Introduction

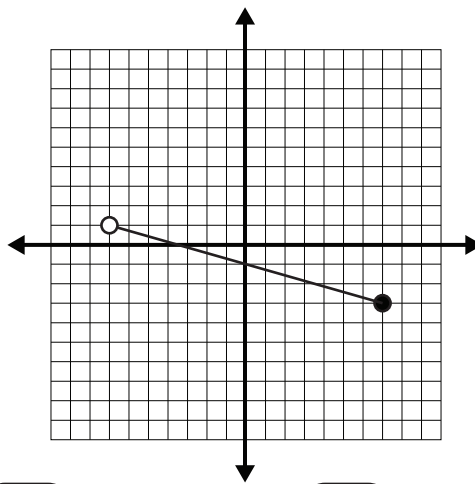
a) Write the domain and range of this graph *in sentence form*.



Domain:

Range:

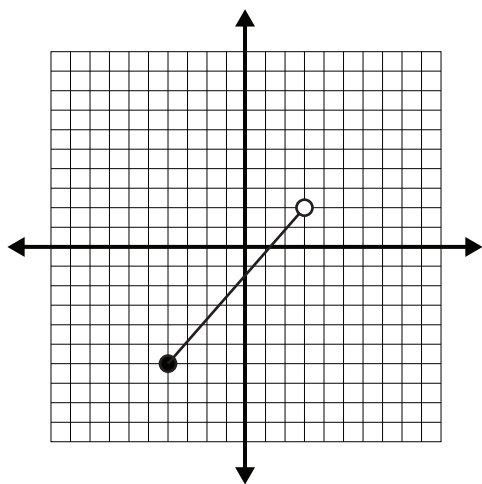
b) Write the domain and range of this graph *as number lines*.



Domain:

Range:

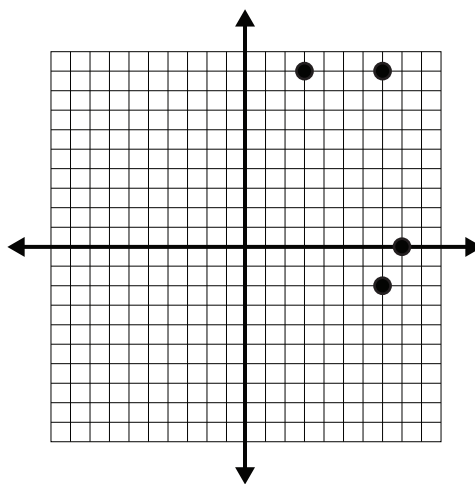
c) Write the domain and range of this graph *in set notation*.



Domain:

Range:

d) Write the domain and range of this graph *as a discrete list*.



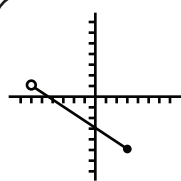
Domain:

Range:

Relations and Functions

LESSON TWO - *Domain and Range*

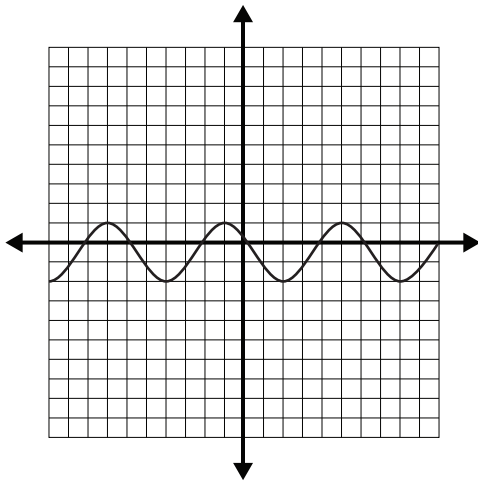
Lesson Notes



Domain
 $\{x \mid -6 < x \leq 3, x \in \mathbb{R}\}$

Range
 $\{y \mid -5 \leq y < 1, y \in \mathbb{R}\}$

e) Write the domain and range of this graph *using interval notation*.

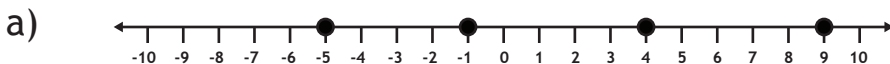


Domain:

Range:

Example 1

Write the domain of each number line.



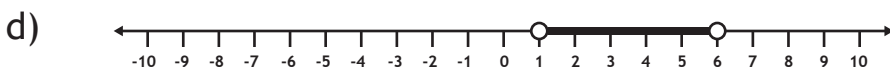
Domain:



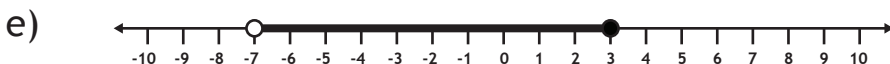
Domain:



Domain:



Domain:



Domain:

Domain
 $\{x | -6 < x \leq 3, x \in \mathbb{R}\}$

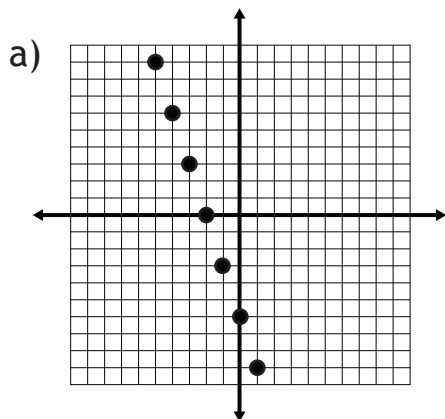
Range
 $\{y | -5 \leq y < 1, y \in \mathbb{R}\}$

Relations and Functions

LESSON TWO - *Domain and Range*

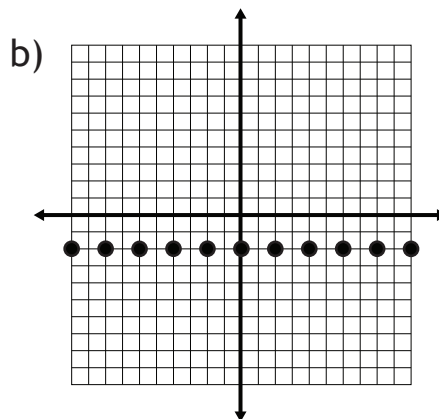
Lesson Notes

Example 2 *domain and range of discrete graphs.*



Domain:

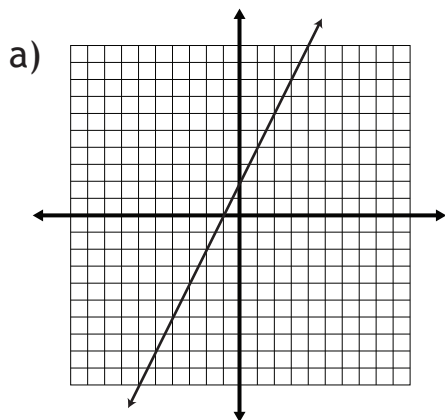
Range:



Domain:

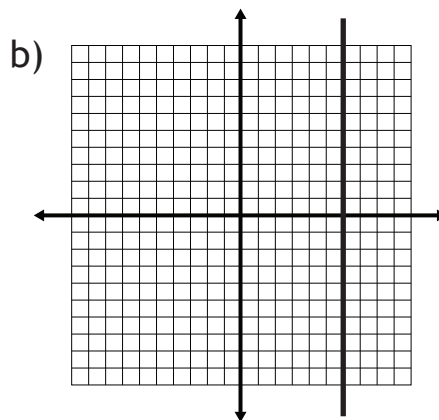
Range:

Example 3 *domain and range of continuous graphs.*



Domain:

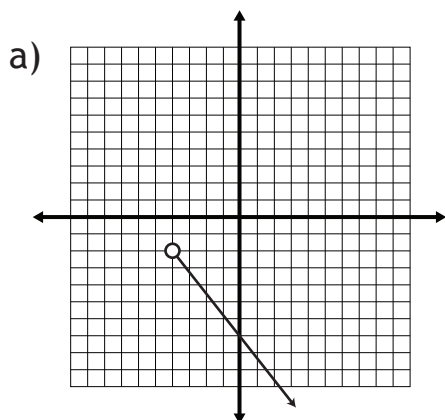
Range:



Domain:

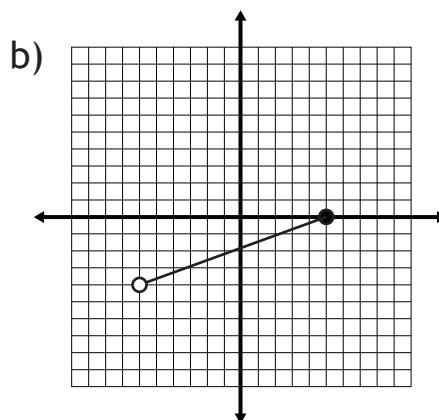
Range:

Example 4 *domain and range of graphs with endpoints*



Domain:

Range:



Domain:

Range:

Relations and Functions

LESSON TWO - *Domain and Range*

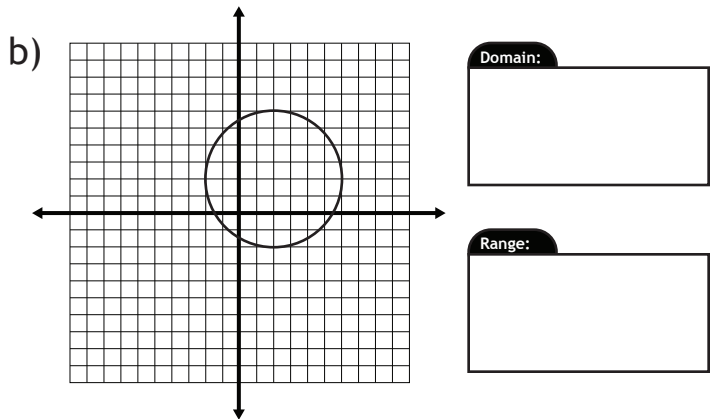
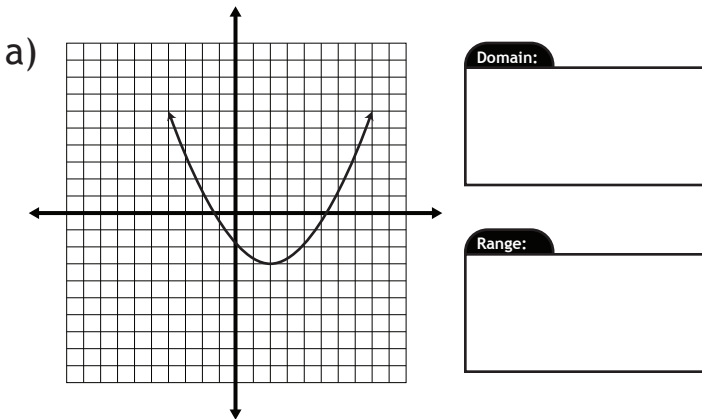
Lesson Notes

Domain
 $\{x \mid -6 < x \leq 3, x \in \mathbb{R}\}$

Range
 $\{y \mid -5 \leq y < 1, y \in \mathbb{R}\}$

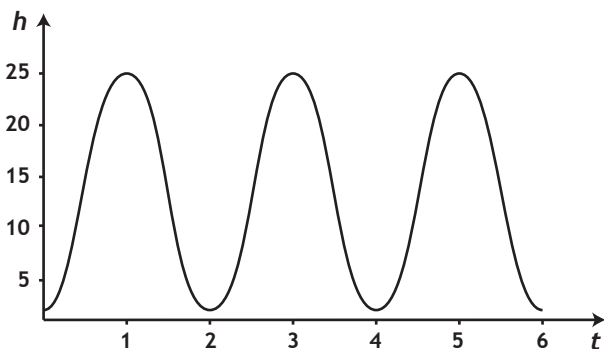
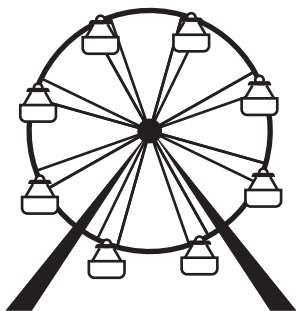
Example 5

domain and range of parabolas and enclosed shapes



Example 6

A Ferris wheel has a radius of 12 m and makes one complete revolution every two minutes. Riders board the wheel at a height of one metre above the ground. A ride lasts for three revolutions of the wheel. The graph of the motion is shown below. State the domain and range, in as many ways as possible.



Sentence

Number Lines

Set Notation

Discrete List

Interval Notation



Relations and Functions

LESSON THREE - *Functions*

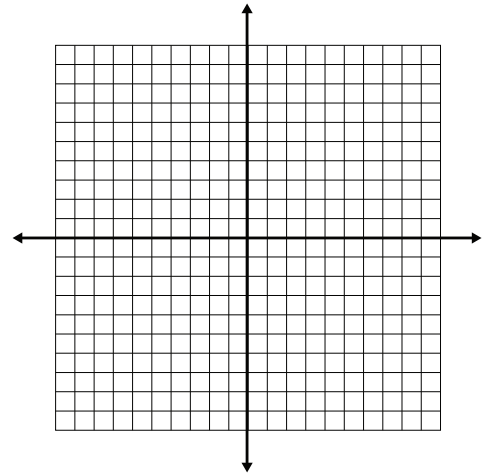
Lesson Notes

Introduction

For each of the following functions, complete the table of values and draw the graph.

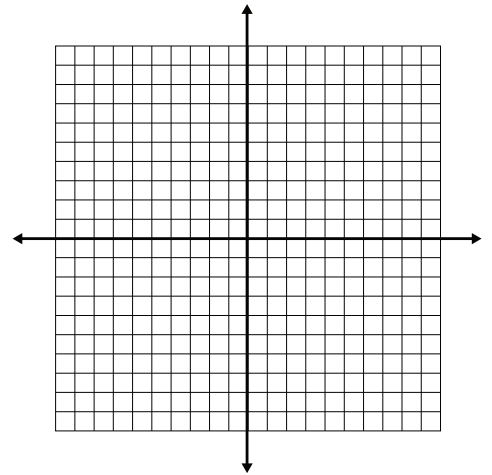
a) $f(x) = x + 4$

x	$f(x)$
-2	
-1	
0	
1	
2	



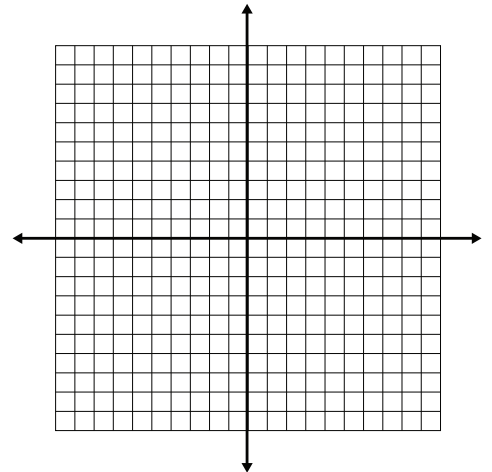
b) $f(x) = 3x - 4$

x	$f(x)$
-2	
-1	
0	
1	
2	



c) $f(x) = x^2 - 3$

x	$f(x)$
-2	
-1	
0	
1	
2	



Relations and Functions

LESSON THREE - *Functions*

Lesson Notes



Example 1

For each function, calculate $f(3)$.

a) $f(x) = -3x - 7$

d) $f(x) = x^2 - 2$

b) $f(x) = \frac{5}{3}x + 2$

e) $f(x) = (x - 1)^2$

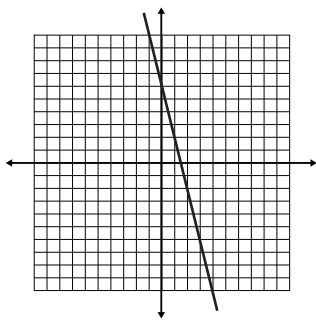
c) $f(x) = -\frac{1}{3}x - 3$

f) $f(x) = 2x^3 - 5x^2 + x - 7$

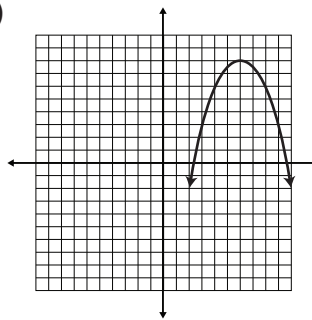
Example 2

Use the graph of each function to determine the value of $f(3)$.

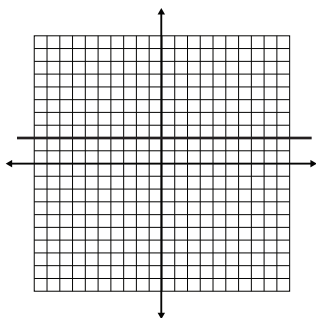
a)



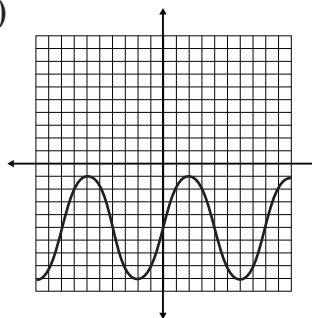
c)



b)



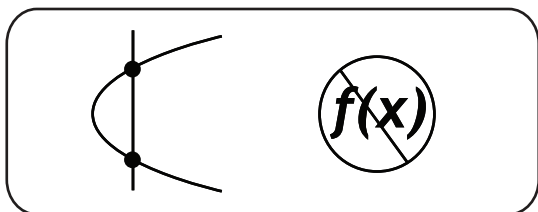
d)



Relations and Functions

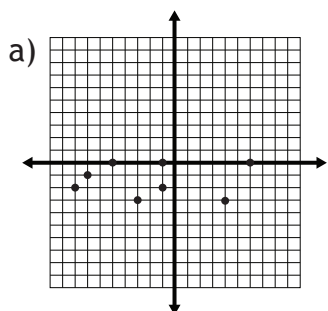
LESSON THREE - *Functions*

Lesson Notes

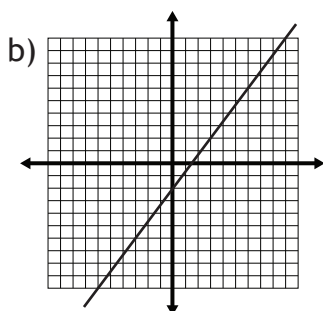


Example 3

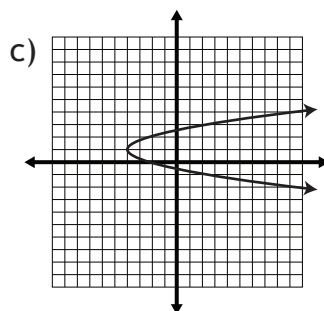
Determine which of the following graphs represents a function.



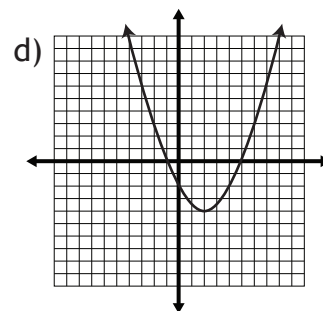
Function: Yes No



Function: Yes No



Function: Yes No



Function: Yes No

Example 4

a) Given $f(x) = 5x + 2$, the point $(k, 12)$ exists on the graph. Find k .

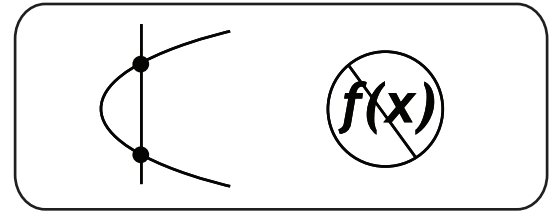
b) Given $f(x) = -\frac{3}{4}x + 5$, the point $(k, -13)$ exists on the graph. Find k .

c) Does the point $(-11, 81)$ exist on the graph of $f(x) = -7x + 3$?

Relations and Functions

LESSON THREE - *Functions*

Lesson Notes



Example 5

A speed walker walks with a speed of 6 km/hour.

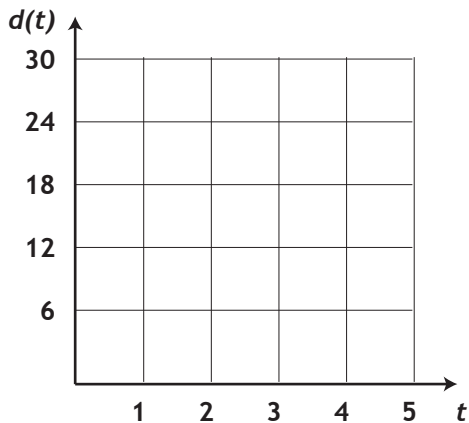
a) Use a table of values to determine the distance walked in the first five hours.

t	d
0	
1	
2	
3	
4	
5	

b) Write the distance function.

<i>Distance Function</i>

c) Draw the graph of this function.
Is the graph continuous or discrete?



d) State the dependent and independent variables.

dependent:
independent:

e) Write the domain and range.

Domain:	Range:

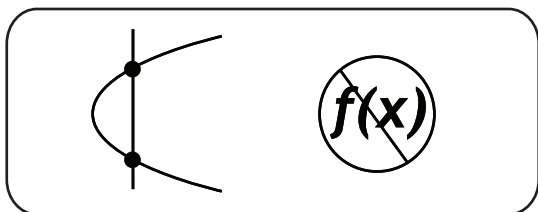
f) How far does the speed walker travel in 1.4 hours?

g) How long does it take for the speed walker to walk 15.6 km?

Relations and Functions

LESSON THREE - *Functions*

Lesson Notes



Example 6

The cost of a sandwich is \$4.40 with two toppings, and \$5.00 with five toppings.

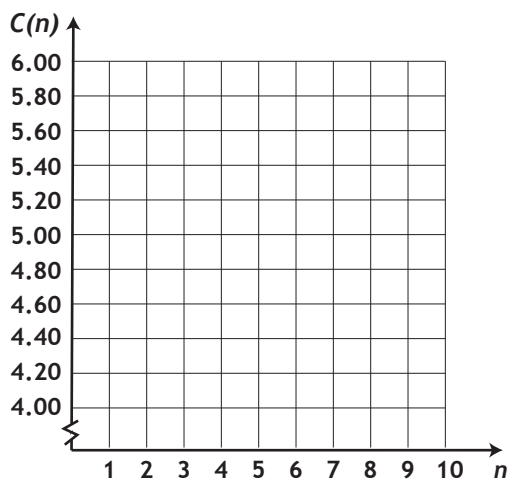
a) Use a table of values to determine the cost of the sandwich for the first five toppings.

n	C
0	
1	
2	
3	
4	
5	

b) Write the cost function.

Cost Function

c) Draw the graph of this function. Is the graph continuous or discrete? There are 10 toppings available.



d) State the dependent and independent variables.

dependent:

independent:

e) Write the domain and range.

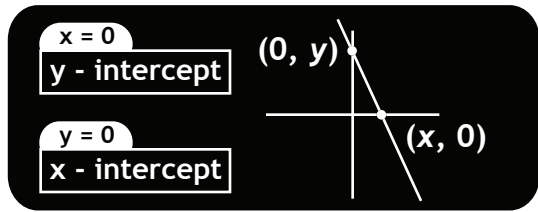
Domain:

Range:

f) What is the price of a sandwich with seven toppings?

g) How many toppings are on a \$5.80 sandwich?

This page is left blank intentionally for correct page alignment.



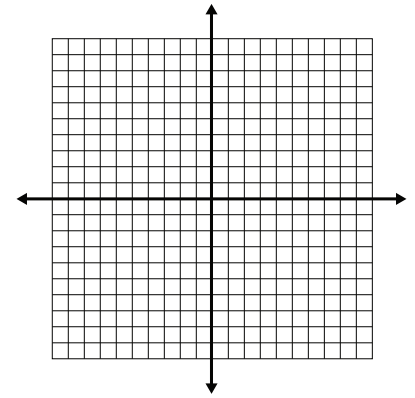
Relations and Functions

LESSON FOUR - *Intercepts*

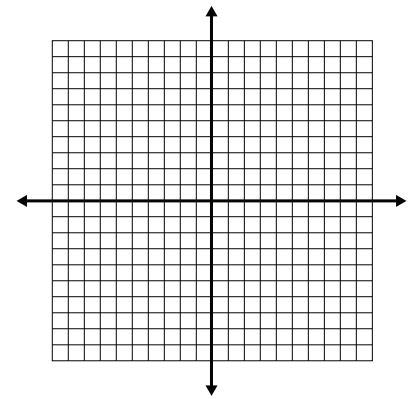
Lesson Notes

Introduction Find the intercepts and draw the graph.

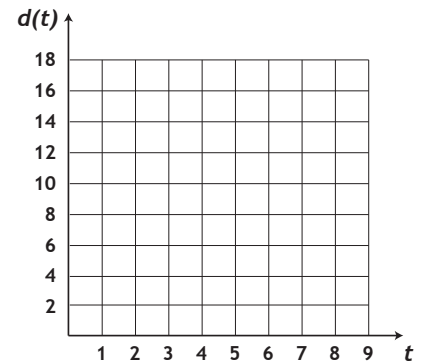
a) $y = 4x - 8$



b) $f(x) = \frac{2}{3}x + 2$



c) $d(t) = -2t + 18$



Example 1

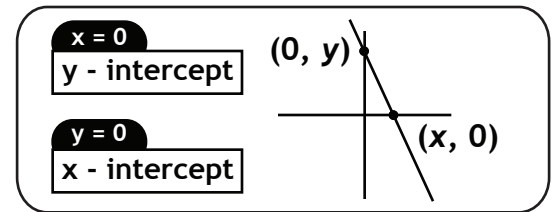
a) The function $f(x) = 2x + k$ has a y-intercept of -5. Find the value of k .

b) The function $f(x) = 3x + k$ has an x-intercept of -2. Find the value of k .

Relations and Functions

LESSON FOUR - *Intercepts*

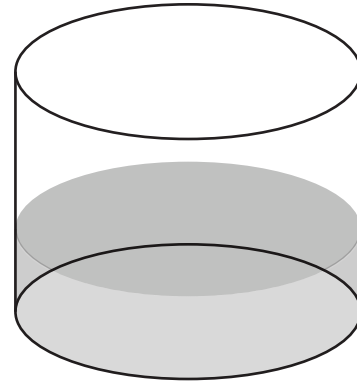
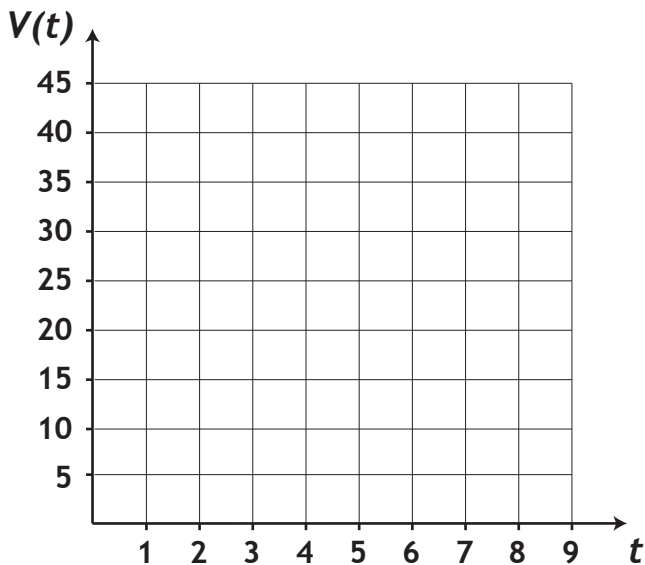
Lesson Notes



Example 2

A cylindrical tank with 45 L of water is being drained at a rate of 5 L/min.

a) Graph the volume of the tank.



b) Write a function to represent this scenario.

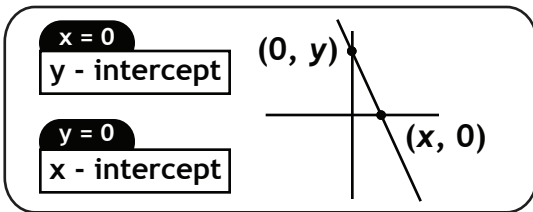
c) What does each intercept represent?

d) State the domain and range.

Relations and Functions

LESSON FOUR - *Intercepts*

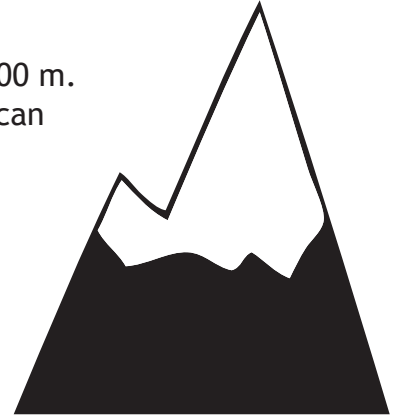
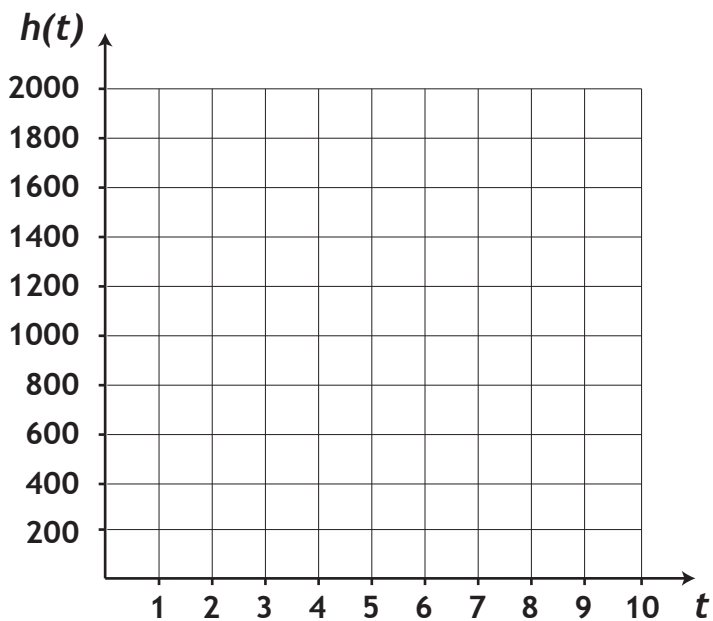
Lesson Notes



Example 3

A mountain climber is at the peak of a mountain with an altitude of 1400 m. It takes 8 hours for the climber to return to ground level. The climber can descend the mountain at an average speed of 175 m/hour.

a) Graph the height of the mountain climber.

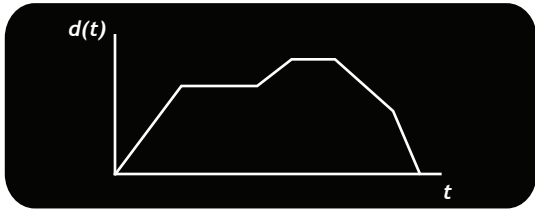


b) Write a function to represent this scenario.

c) What does each intercept represent?

d) State the domain and range.

This page is left blank intentionally for correct page alignment.

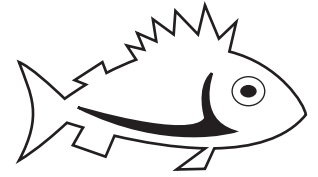


Relations and Functions

LESSON FIVE - *Interpreting Graphs*

Lesson Notes

Introduction



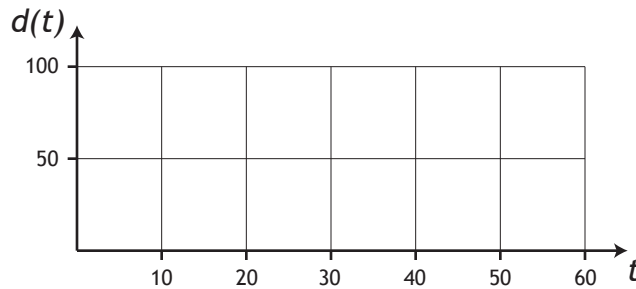
In a 100 m fish race, there are three competitors.

Teleporting Fish - has the ability to instantly warp from location to location.

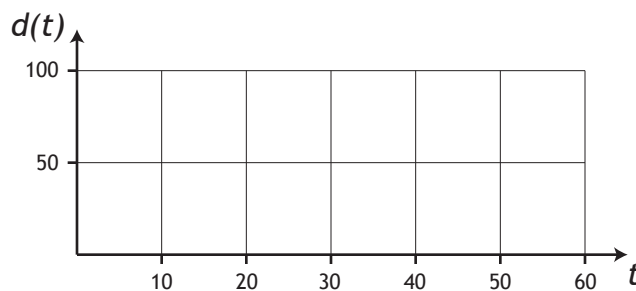
Instant-Speed Fish - can reach any desired speed instantly without accelerating.

Real-World Fish - must speed up and slow down, just like objects in reality.

a) Teleporting Fish spends the first 20 s of the race resting at the start line. He then warps to the midpoint of the track and rests for another 20 seconds. Finally, he warps to the end and waits 20 seconds while the other fish arrive. Graph this motion.

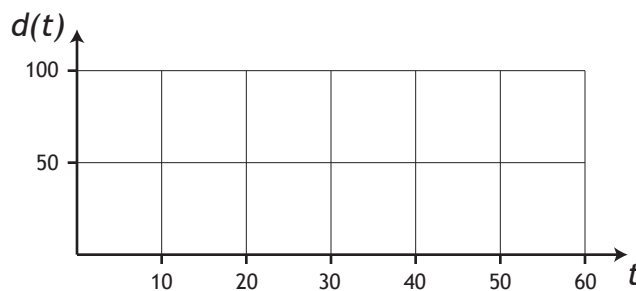


b) Instant-Speed Fish begins the race at 2.5 m/s, and sustains that speed for 20 seconds until she reaches the midpoint. After resting for 20 seconds, she resumes her speed of 2.5 m/s and heads to the finish line.



c) Real-World Fish accelerates to a speed of 2.5 m/s in 6 seconds, holds that speed for 8 seconds, and then decelerates to zero in 6 seconds - this brings him to the midpoint.

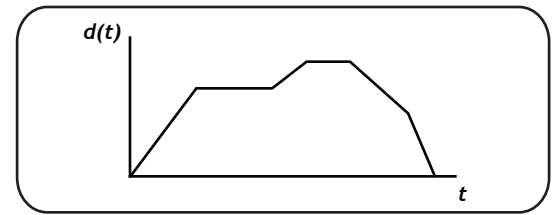
After resting for 20 seconds, Real-World fish repeats the motion - accelerate for 6 seconds, hold the speed for 8 seconds, and decelerate for 6 seconds. This brings him to the finish line.



Relations and Functions

LESSON FIVE - *Interpreting Graphs*

Lesson Notes



Example 1

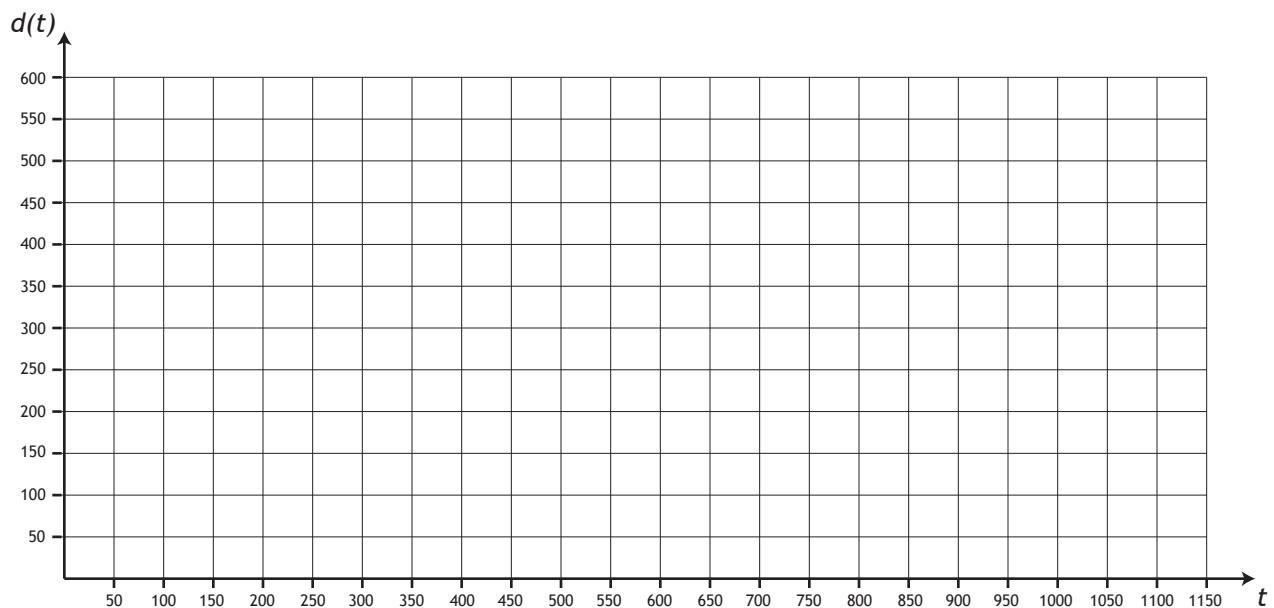
Alex walked halfway to school, but realized he forgot his calculator. He turned around, ran back home, and searched his room for five minutes trying to find the calculator. He then ran two-thirds of the way back to school, but got tired and had to walk the remaining third. Draw a graph representing Alex's journey. Assume instant speed changes.

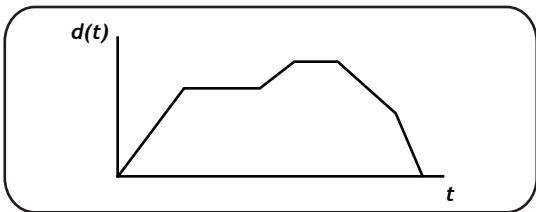
Distance from home to school	600 m
Alex's running speed	2 m/s
Alex's walking speed	1 m/s

Drawing the graph exactly requires calculations using $\text{time} = \frac{\text{distance}}{\text{speed}}$.

Find ordered pairs that will let you draw the graph. Use the space below for your work.

i) walking to school	ii) running back home	iii) looking for calculator	iv) running to school	v) walking to school





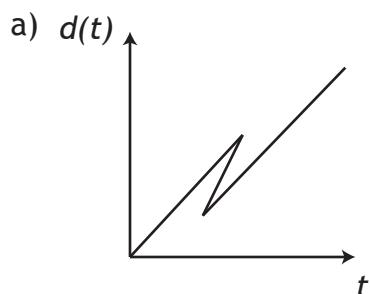
Relations and Functions

LESSON FIVE - *Interpreting Graphs*

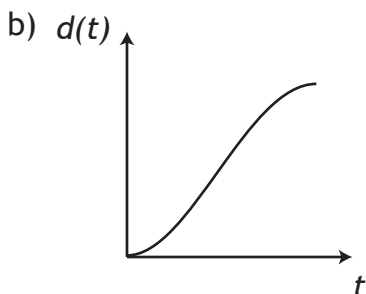
Lesson Notes

Example 2

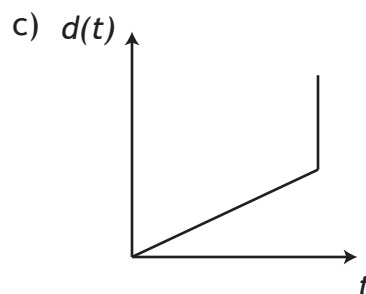
Each of the following graphs represents a potential path Naomi can take from home to school. Determine if each graph represents a possible or impossible motion.



Possible: Yes No



Possible: Yes No

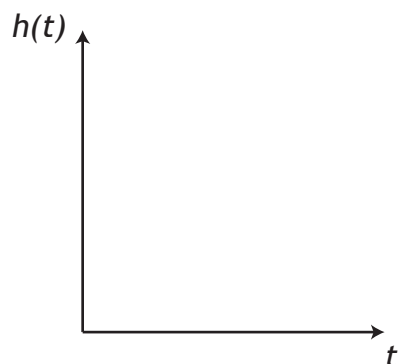


Possible: Yes No

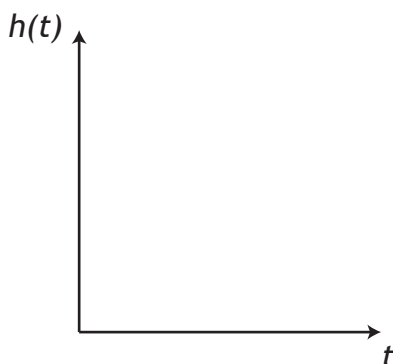
Example 3

Represent each of the following motions in graphical form.

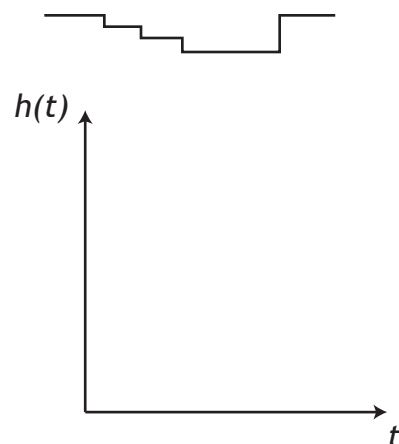
a) A ball is thrown straight up and falls back down.



b) A rubber ball is dropped and bounces three times.



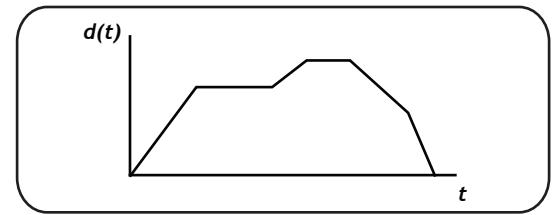
c) The swimming pool below is filled with water.



Relations and Functions

LESSON FIVE - *Interpreting Graphs*

Lesson Notes



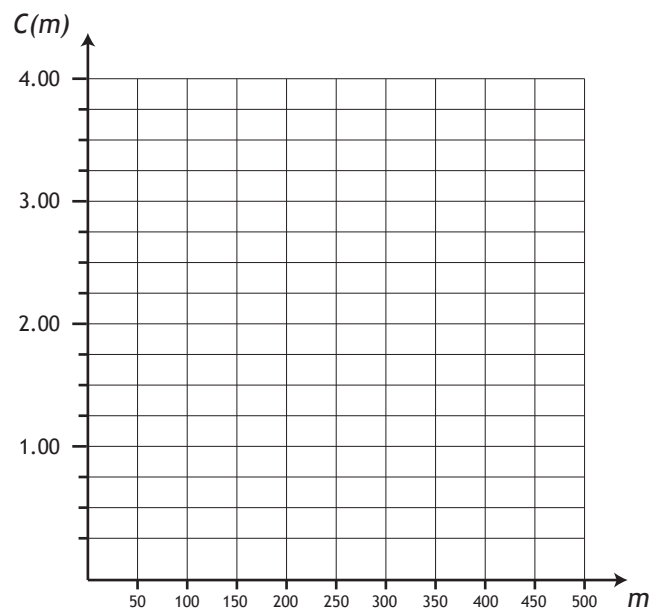
Example 4

The following table shows the Canada Post 2010 price list for mailing letters within Canada.

Letter Mass	Price
up to (and including) 30 g	\$0.57
up to (and including) 50 g	\$1.00
up to (and including) 100 g	\$1.22
up to (and including) 200 g	\$2.00
up to (and including) 300 g	\$2.75
up to (and including) 400 g	\$3.00
up to (and including) 500 g	\$3.25



a) Graph this data



b) State the domain and range

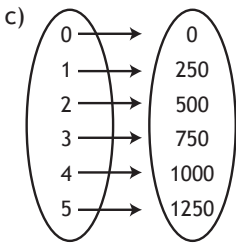
Domain:

Range:

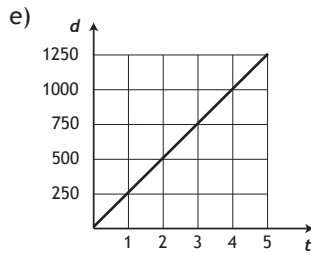
Relations and Functions Lesson One: Graphing Relations

Introduction:

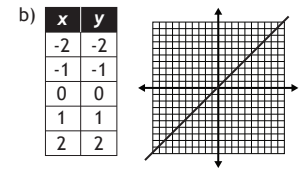
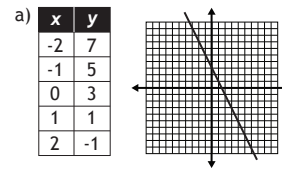
a) Caitlin bikes 250 metres for every minute she travels. b) $\{(0, 0), (1, 250), (2, 500), (3, 750), (4, 1000), (5, 1250)\}$



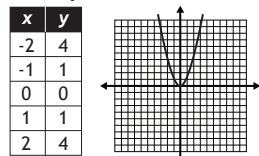
d) $d = 250t$



Example 1:

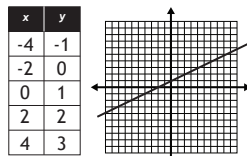


Example 2: a)



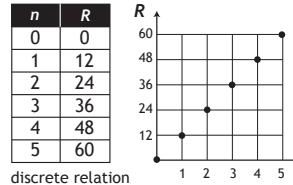
non-linear relation

b)

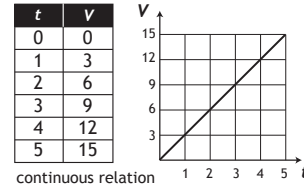


linear relation

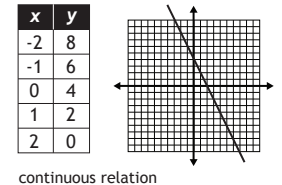
Example 4:



Example 5:



Example 6: $y = -2x + 4$



Example 3:

a) dependent variable: R , independent variable: n , rate: \$3/box, equation: $R = 3n$

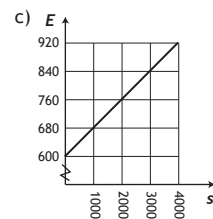
b) dependent variable: d , independent variable: t , rate: 9 m/s, equation: $d = 9t$

c) dependent variable: P , independent variable: d , rate: 10 kPa/m, equation: $P = 10d$

Example 7: a) $E = 0.08s + 600$

b)

s	E
0	600
1	680
2	760
3	840
4	920



d) linear

e) continuous

f) earnings is dependent, sales is independent.

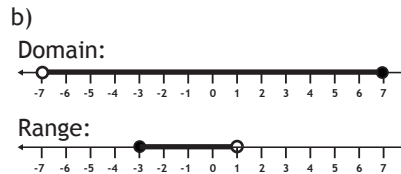
g) \$1 096

h) \$12 000

Relations and Functions Lesson Two: Domain and Range

Introduction:

a)
Domain: All real numbers between -4 and 0, but not including -4.
Range: All real numbers between -1 and 8, but not including -1.



c) Domain: $\{x \mid -4 \leq x < 3, x \in \mathbb{R}\}$
Range: $\{y \mid -6 \leq y < 2, y \in \mathbb{R}\}$

d) Domain: $\{3, 7, 8\}$
Range: $\{-2, 0, 9\}$

e) Domain: $(-\infty, \infty)$
Range: $[-2, 1]$

Example 1: a) $\{-5, -1, 4, 9\}$ b) $\{n \mid n \geq -3, n \in \mathbb{R}\}$ c) $\{n \mid n < -1, n \in \mathbb{R}\}$ d) $\{n \mid 1 < n < 6, n \in \mathbb{R}\}$ e) $\{n \mid -7 < n \leq 3, n \in \mathbb{R}\}$

Example 2: a) $\{-5, -4, -3, -2, -1, 0, 1\}$, $\{-9, -6, -3, 0, 3, 6, 9\}$ b) $\{-10, -8, -6, -4, -2, 0, 2, 4, 6, 8, 10\}$, $\{2\}$ • Example 3: a) $x \in \mathbb{R}, y \in \mathbb{R}$ b) $x=6, y \in \mathbb{R}$

Example 4: a) $x > -4, y < -2$ b) $-6 < x \leq 5, -4 < y \leq 0$ • Example 5: a) $x \in \mathbb{R}, y \geq -3$ b) $-2 \leq x \leq 6, -2 \leq y \leq 6$

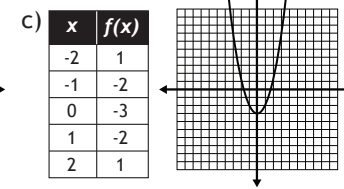
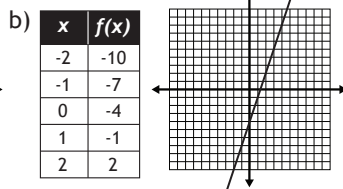
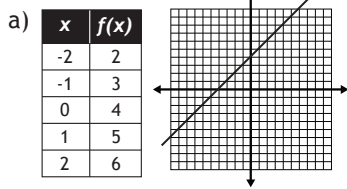
Example 6: Sentence: The domain is between 0 and 6, and the range is between 1 and 25. Set Notation: $0 \leq t \leq 6, 1 \leq h \leq 25$

Number Lines: Domain: Range: Intervals: $[0, 6], [1, 25]$

Answer Key

Relations and Functions Lesson Three: Functions

Introduction:



Example 1: a) -16 b) 7 c) -4
d) 7 e) 4 f) 5

Example 2: a) -6 b) 2 c) 3 d) -2

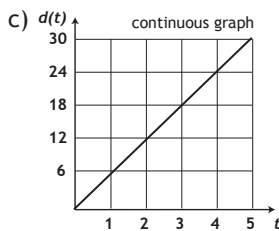
Example 3: a) no b) yes
c) no d) yes

Example 4: a) 2 b) 24 c) no

Example 5:

a)

t	d
0	0
1	6
2	12
3	18
4	24
5	30



d) dependent: d
independent: t

e) $t \geq 0, d \geq 0$

f) 8.4 km

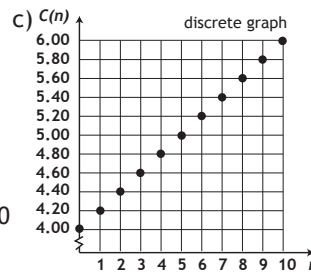
g) 15.6 km

b) $d(t) = 6t$

Example 6:

a)

n	C
0	4.00
1	4.20
2	4.40
3	4.60
4	4.80
5	5.00



d) dependent: C
independent: n

e) Domain: {0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10}
Range: {4.00, 4.20, 4.40, 4.60, 4.80, 5.00, 5.20, 5.40, 5.60, 5.80, 6.00}

f) \$5.40

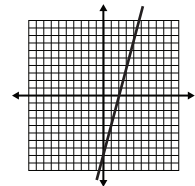
g) 9

b) $C(n) = 0.20n + 4.00$

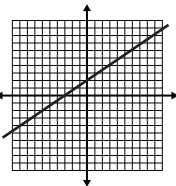
Relations and Functions Lesson Four: Intercepts

Introduction:

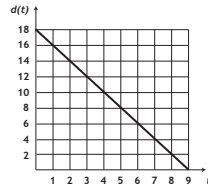
a) x-intercept: (2, 0)
y-intercept: (0, -8)



b) x-intercept: (-3, 0)
y-intercept: (0, 2)



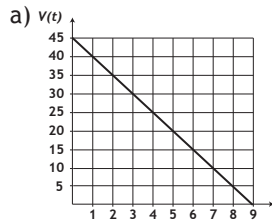
c) t-intercept: (9, 0)
d-intercept: (0, 18)



Example 1:

a) $k = -5$ b) $k = 6$

Example 2:

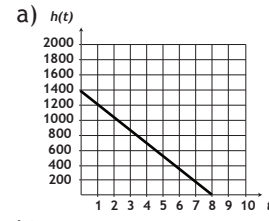


b) $V(t) = -5t + 45$

c) The V-intercept is the initial volume of water. The t-intercept is the time when the tank is empty

d) $0 \leq t \leq 9, 0 \leq V \leq 45$

Example 3:



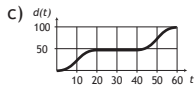
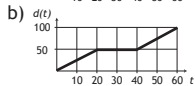
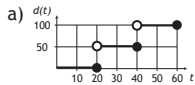
b) $h(t) = -175t + 1400$

c) The h-intercept is the initial height of the climber (1400 m). The t-intercept is the time the climber reaches the ground (8 hours).

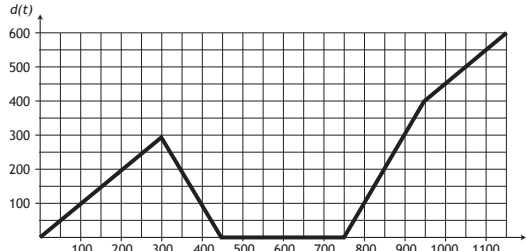
d) $0 \leq t \leq 8, 0 \leq h \leq 1400$

Relations and Functions Lesson Five: Interpreting Graphs

Introduction:



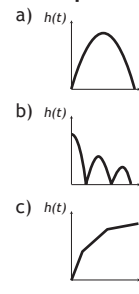
Example 1:



Example 2:

a) impossible
b) possible
c) impossible

Example 3:



Example 4:

